In-the-Spectacle-Lens Telescopic Device

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**ABSTRACT**

Spectacle mounted telescopic systems are prescribed for individuals with visual impairments. Bioptic telescopes are typically mounted toward the top of spectacle lens or above the frame with the telescope eyepiece positioned above the wearer’s pupil. This allows the wearer to alternate between the magnified narrow field-of-view (available through the eyepiece) and the unmagnified wide view (through the carrier lens) using head motion. Rejection of this visual aid has been attributed mainly to its appearance and to limited field-of-view through the smaller Galilean designs. We designed a wide-field Keplerian telescope that is built completely inside the spectacle lens. The design uses embedded mirrors inside the carrier lens for optical pathway folding and conventional lenses or curved mirrors for magnification power. The short height of the ocular, its position, and a small tilt of the ocular mirror enable the wearer to simultaneously view the magnified field above the unmagnified view of the uninterrupted horizontal field. These features improve the cosmetics and utility of the device. The in-the-lens design allows the telescopes to be mass-produced as a commodity ophthalmic lens blank that can be surfaced to include the wearer prescription.

**Keywords:** Visual multiplexing, bioptic telescope, optical visual aid, low vision, macular degeneration, vision rehabilitation, driving aids.
1. Background

Magnification is useful for individuals who suffer from loss of resolution or contrast sensitivity, due to defects in the optics of the eye or retina. Damage to the fovea (the central part of the retina) is common in age related macular degeneration (AMD) and many other diseases. This impairment dramatically affects an individual’s ability to read, recognize faces and other fine discrimination tasks. As the population ages the number of people affected by this and other eye diseases with similar impact is expected to grow rapidly.

It is possible to provide sufficient magnification for reading and other tasks performed within arm length using high power reading glasses, hand- and stand-optical magnifiers (using standard lenses, combined standard and binary optics), fiber optics tapers, and electronic magnifiers that use a camera and a display. A variety of telescopic devices are used for magnification of distant objects including hand-held, head-mounted, and spectacle-mounted telescopes. Both Galilean and Keplerian designs have been used for these devices, and for intermediate distances manual and electronic auto-focus mechanisms have been implemented.

The most successful telescopic low vision devices are bioptic telescopes. Bioptic telescopes are mounted through the spectacle lens (the carrier lens). The telescope’s eyepiece (ocular lens) is usually positioned above the pupil of the wearer. The telescope is tilted up by about 10 degrees (Figure 1). This allows the wearer to look under the telescope eyepiece using their unaided vision through the carrier lens most of the time. When the wearer notes an object of interest through the carrier lens that is not resolvable, a slight head tilt can bring the object into view through the telescope providing the needed magnification. This mode of operation (providing magnification on demand) was termed temporal multiplexing.

Bioptic telescopes are permitted as driving visual aids for people with low vision in 36 states in the USA. When driving (a relatively demanding task), wearers report looking through
the telescope only about 5% of the time \textsuperscript{8}. In other tasks the telescope may be used even less frequently.

![Figure 1: A monocular Galilean bioptic telescope. a) Most of the time the wearer views through the carrier lens without any effect of the telescope. b) With a slight downward tilt of the head the telescope is brought into the line of sight enabling magnified view of the object of interest. The telescope shown is the 3.0× Mini focusable Keplerian bioptic made by Ocutech, Inc. (Chapel Hill, NC)](image)

Through the first part of the 20\textsuperscript{th} century many patents were filed disclosing bioptic telescopes for the treatment of low vision in the US and Europe. \textsuperscript{9-11}. However, the devices were made popular and effective through the efforts of William Feinbloom who was the first to promote them as a driving aid \textsuperscript{12}.

Early bioptics were fixed-focus Galilean designs that facilitated small and light weight devices. The emphasis on small, compact designs resulted in narrow fields of view (e.g., about 9\textdegree{} in a 3× telescope\textsuperscript{13} \textsuperscript{14}) and generally provided relatively dim images. Eventually Keplerian-based bioptic telescopes were developed that provided brighter images and wider fields of view (e.g., 13\textdegree{} in a 3× telescope\textsuperscript{13}). The Keplerian telescopes were larger and heavier due to the inherently longer optical path and the need for image erecting components.
Although bioptic telescopes can be effectively used in a variety of settings\textsuperscript{15}, many visually impaired people reject them\textsuperscript{16}. The obvious and unsightly appearance of these prosthetic devices has been identified as one major reason for the reluctance of people with vision impairments to use bioptic telescopes. The bioptic telescope position also causes it to interfere with eye contact that is crucial for social interactions. Various approaches where taken in attempts to improve the cosmetic appearance of bioptic telescopes including the use of very small Galilean telescopes\textsuperscript{13}, small mostly behind-the-spectacle-lens Keplerian telescopes\textsuperscript{17,18}, and horizontal telescopes folded above the spectacle lenses\textsuperscript{19}. While each of these devices attempts to address the cosmetic issues hindering the bioptic telescope, they remain obtrusive and many patients who could benefit from their use continue to reject them. In addition, attempts at miniaturization\textsuperscript{20,21} invariably result in optical compromises including reductions in field-of-view or image brightness, or both.

A somewhat less noticeable telescope can be created by combining a high negative power contact lens\textsuperscript{22} or surgically implanted intra-ocular lens (IOL)\textsuperscript{23} with a high positive power spectacle lens. Such telescopes have limited magnification though 3.0× is possible. While they may have a slightly wider field-of-view then spectacle mounted telescopes, they severely restrict eye scanning ability by stabilizing the image on the retina\textsuperscript{24,25}. Because the system nodal point is close to the eye’s center of rotation eye movements do not result in retinal image movements\textsuperscript{26}. Therefore all image scanning has to be done by head movements. Additionally, the high power spectacle lens magnifies the wearer’s eyes and thus interferes with social eye contact. Patients rejected the cosmetics of the contact lens-spectacle system due to the unsightly appearance of the high power spectacle lens\textsuperscript{27}. We believe that the image stabilization was also a cause for rejection of these devices as might be the full time field restriction imposed by these systems (when used binocularly, as they were designed). A bifocal intraocular implantable lens (IOL) was developed to be used either with high power spectacle lens for magnification or without it for non magnified\textsuperscript{28}. The large size and poor cosmetics of doublet spectacle lens used
with these devices is believed to be the reason for the rejection of such systems by wearers, despite success in optical performance reported 28. Here too the retinal image stabilization prevented eye scanning. Using a small high power inset lens in a normal looking carrier lens in combination with the bifocal IOL 29 might overcome both the cosmetics and image scanning limitation of this approach. A fully implanted intra-ocular telescope is now available which offers normally looking spectacles and eyes but requires a surgical procedure 30, 31. The telescope is implanted in one eye leaving the second eye for mobility tasks, it provides dimmer retinal images in comparison with spectacle mounted telescopes, and may interfere with eye examination and treatment. This miniature telescope also has limited field-of-view, though not as limited as comparable spectacle mounted bioptics, and it permits natural eye scanning 25. The implantable devices have fixed level of magnification preventing a change in power that may be desirable with progression of the vision impairment.

While patients are concerned with the cosmetics of the device, low vision professionals who object to the use of the bioptic telescope while driving frequently raise the presence of a ring shaped scotoma (blind area) around the magnified image (Fig.2a) as a cause for concern 32, 33. The blind area is a direct result of the magnification of the field-of-view of the telescope spread over a larger retinal area and consequently prevents that retinal area from imaging the surrounding scene.

The ring scotoma problem may be alleviated in two ways. In most cases the bioptic is fitted over one eye (monocularly). It has been argued that the other eye, if functional, can continue to monitor the area corresponding to the ring scotoma and thus avoid this potential difficulty 12, 34. We have termed that situation bi-ocular multiplexing 6. A second way of eliminating the ring scotoma may be applied to both monocular and binocular telescopes. When looking through the bioptic telescope the wearer can simultaneously view the magnified image of an object together with the unmagnified image of the rest of the scene except for the ring scotoma (Fig. 2a). With a small field of view, a telescope that is misaligned with the eye’s
optical axis can present a magnified image of an object immediately above the view of the same object through the carrier lens (Fig. 2b). This method of dealing with the ring scotoma of the bioptic telescope was termed ‘Simulvision’ and was described with the introduction of the bi-level telemicroscopic apparatus (BITA) micro Galilean bioptic telescope 35. Simulvision is an example of spatial multiplexing by shifting 6.

Figure 2: A simulated view of a road sign viewed through a 3.0× telescope.  
a) The view through a conventional bioptic. The magnified image on the retina blocks the view of much of the intersection creating a ring scotoma (blind area). b) The rectangle field-of-view through the in-the-lens telescope. The magnified image is shifted up blocking part the view of the pedestrian bridge overhead but leaves the intersection in full view. Note the non magnified view of the road sign seen under the magnified view. The white line surrounding the magnified image is only added to make the illustration more clear.

In this manuscript we describe a low vision bioptic telescope designed to overcome many of the limitations of previous designs by building the telescope into the spectacle lens 36. This design can provide a relatively wide field-of-view, high-magnification, and bright-image while
decreasing aesthetic distinction from other eyewear. This document will also show that the new
design also lends itself to spatial multiplexing by shifting, to a wide field-of-view horizontally
and to increased light efficiency.

2. Optical Designs

The principal novelty of the in-the-lens telescope is that the optical elements composing a
terrestrial telescope are embedded within the carrier spectacle lens. This requires that the optical
path is folded so that it is mostly orthogonal to the visual axis of the spectacles, and light is
transmitted through the carrier lens body. We describe a series of designs and implementations
below.

2.1. Periscopic Galilean with laminated lenses

The basic Galilean telescope folded into the lens is shown schematically in Fig.3. A
carrier lens of thickness $t$ is shown in a view from above as a rectangle. A positive lens serving
as the objective and a negative lens of higher power serving as the ocular are shown laminated to
the carrier lens. A pair of plane mirrors serves as a periscope to move the image from the
objective to the ocular across the carrier lens.
Figure 3: a) A basic schematic design of the in-the-lens telescope with a spectacle lens of thickness, $t$ seen from above. For the Galilean design a positive objective lens and a negative ocular lens are laminated to the carrier lens. Two mirrors serve to periscopically pass the image from the objective to the ocular. b) An illustration of the in-the-lens when the wearer looks though the carrier lens. c) The same lens following a head tilt that brings the telescope in front of the pupil. Note the thin and tall shape of the telescopic mirrors due to the limitation by the carrier lens thickness on the width of the mirrors.

The most important design parameter for a bioptic telescope is the magnification. The angular magnification $M$ of an afocal Galilean telescope, as shown in Fig. 3, is determined by the ratio of the object focal length of the objective lens $f_{ob}$ (negative in this case) to the image focal length of the ocular lens $f'_{oc}$ (also negative since the ocular is divergent):

$$M = \frac{f_{ob}}{f'_{oc}}. \quad (1)$$

In the case of a Galilean telescope $M$ is positive, meaning the final image is erected (not inverted).
The afocal condition is achieved when the distance between objective and ocular lenses, called tube length $L$, is equal to the difference of the focal lengths of both lenses. In this embedded design, light travels through the carrier lens of refractive index $n$. Under the thin-lens approximation, it is generally derived as:

$$L = f'_{ob} - f'_{oc} = -nf'_{ob} + nf'_{oc} = n(1 - M)f'_{oc}.$$  \hspace{1cm} (2)

Attending to the sign of focal lengths in the case of the Galilean telescope, it results as:

$$L = n(M - 1)|f'_{oc}|.$$  \hspace{1cm} (3)

Bioptic telescopes range in magnification form $1.5\times$ to $8.0\times$ with $3.0\times$ to $4.0\times$ used most commonly. The second most important parameter for a bioptic telescope is the field-of-view (FOV). Either the objective or the ocular may serve as the limiting aperture in a Galilean telescope. The FOV, on the retina of the wearer, is determined by either the angle spanned at the pupil by the ocular lens or the angle spanned by the image of the objective as seen through the ocular; the smaller of these two angles is the FOV. In the design of the Galilean telescope shown in Fig. 3a, the carrier lens thickness limits the periscopic mirrors’ width but not their height. Since we would like to keep the carrier lens as thin as practical for cosmetic and weight considerations, the field of such a telescope is likely to be taller than it is wide (Fig. 3b). This is less than optimal as the width of the FOV is considered more important for bioptics than the height. In addition, the exit pupil, the image of the objective formed by the ocular, is smaller than the objective itself, since the lateral magnification is $1/M$.

The second factor affecting the FOV is the distance between the field limiting aperture and the eye’s pupil. Since the device is meant to be embedded in spectacle glasses, the distance from the last surface to the eye should be as similar as possible to that of conventional spectacle ophthalmic lenses. This vertex distance is usually 12 to 14mm. In the case of the Galilean design the exit pupil of the telescope lies within the telescope. Generally, the exit pupil acts as a
field limiting aperture and since the eye can never be placed in the same plane, it limits the FOV and also causes vigneting by reducing the light reaching the pupil from eccentric objects.

2.2. **Keplerian design with laminated lenses**

A Keplerian configuration in bioptics has a number of advantages over the Galilean design as described below. The main disadvantages of a Keplerian bioptics are the larger dimension of the telescope (for the same magnification and objective lens power) and the need of an optical erecting element that adds weight or other complications. However, both limitations are easily overcome with the proposed in-the-lens design. Fig. 4 shows side and front view schematic illustrations of a Keplerian in-the-lens telescope. The spectacle carrier lens (dotted line) has a thickness $t$. The ocular and objective lenses are laminated to the carrier lens surfaces. Arrows show the direction light travels across the 4 embedded erecting mirrors arranged in a configuration similar to the reflections obtained in the Abbé's version of the Porro prisms 38 (also called 2nd kind Porro prisms). Following a head tilt to align the telescope with the eye, the ocular and $M4$ are placed in front of the wearer’s eye (as shown in Fig 4b). At other times the wearer can view through the carrier lens, under mirror $M4$, providing an unimpeded field-of-view.

The same computations (Eq. 1 and 2) apply to a Keplerian telescope with the only difference being the sign of the ocular focal length (positive), resulting in the tube length being equal to the sum of the focal lengths of both lenses

$$L = f_{ob}' - f_{oc}' = n (1 + |M|) f_{oc}' .$$  

(4)

Thus, a longer optical path is required for a Keplerian design. This additional length is not difficult to achieve as the Keplerian design needs erecting mirrors which naturally expands the optical path through the carrier lens.

The orientation of the Mirrors ($M1$ and $M2$) in the Keplerian design is such that their height is limited by the carrier lens thickness but not their width (horizontal dimension). The FOV of a Keplerian telescope is limited only by the size of the ocular lens. Thus the Keplerian
design in-the-lens telescope has an added advantage that the width of the FOV may be large even with a fairly thin carrier lens.

Figure 4: a) Side view of the Keplerian telescope with laminated lenses and four flat erecting mirrors. b) Front view illustration of the Keplerian design telescope that emphasizes the wide but short configuration of the mirrors and their corresponding field-of-view. In this design the carrier lens thickness limits the height but not the width of the objective and ocular mirrors.

The eye relief is in this case positive, with the exit pupil outside the telescope, allowing the eye pupil to be conjugated with the exit pupil. Therefore the field limiting aperture is now the ocular. This is better than the Galilean design in two ways. First, the distance from the aperture to the eye is reduced (increasing the angular span of the field), and second, the dimension of the limiting aperture (the ocular itself) is not affected by the magnification.

The Keplerian design also lends itself well to Simulvision. Tilting mirror $M4$ (in Fig. 4a) a few degrees clockwise will shift the magnified image up as illustrated in Fig. 2b. An angular displacement up of $T^\circ$ can be achieved by tilting the $M4$ mirror ($\frac{1}{2}T^\circ$). This provides the wearer an unobstructed, non-magnified view of the environment through the carrier lens at the same time as a magnified image (through the telescope) translated vertically. This provides the wearer
an open wide horizontal FOV under the ocular at the same direction of the object that is seen through the telescope. The magnified image could be shifted in other directions, but shifting the magnified image above the unmagnified view is preferable because the magnified image occupies an area of the carrier lens that is less likely to include obstacles or relevant objects (e.g. the sky). The in-the-lens telescope design facilitates Simulvision, in part, because there is no opaque frame or mounting structure to block the unmagnified view.

The optical elements that act as objective and ocular lenses can be conventional meniscus lenses attached to the carrier lens as shown in Figs 3 and 4. Those lenses could be replaced with curved mirrors, Fresnel lenses, diffractive lenses, or holographic elements. These other elements have a durability advantage as they can be embedded within the carrier lens. Using curved mirrors has several advantages: the mirrors are free of chromatic aberration, all the elements can be embedded into the spectacle lens, and curved mirrors yield more optical power with the same curvature comparing with plano-convex meniscus lenses (reducing the dimension requirements for the carrier lens). Furthermore, the distance between mirrors needed to create an afocal optical system does not depend on the refractive index of the carrier lens, but only on the mirrors focal length.

2.3. **Keplerian design with curved mirrors**

Figure 5 shows top, front, and side views of a Keplerian design in-the-lens telescope using curved mirrors (M1 and M4) to affect both the vergence power and periscopic/erecting functions. Using spherical mirrors in this design with a 45° tilt is impractical, as the astigmatic effect will make the telescope useless. It is possible, however, to use off-axis parabolic mirrors for this design. Such mirrors can provide a sharp magnified image, however, as we will show in section 2.5.1, the off axis imaging results in significant anisotropic spatial distortion (illustrated below). This distortion might be disturbing (mostly during image motion) even if it does not affect functionality.
Figure 5: Top, front, and side views schematic of the in-the-lens telescope using only mirrors embedded in the carrier lens. Curved off-axis parabolic mirrors (M1 & M4) for power and flat mirrors (M2 & M3) for the second image inversion.

2.4. **Keplerian design with beam splitters**

An alternative design for a fully embedded Keplerian in-the-lens telescope without the distortion uses two assemblies of beam splitters in combination with spherical concave mirrors to obtain the optical power and the periscopic mirror effects as shown in Fig. 6. This approach implements a magnifying element similar to that used in MicroOptical’s in-the-lens electronic display (see Fig. 7)\(^{39}\). Light entering the carrier lens at the objective window on the left (Fig. 6) is reflected by the first beam splitter towards the concave mirror to the left. Following reflection at the concave mirror the light passes to the right through the beam splitter traveling through the carrier lens, forming an intermediate image plane, and proceeding through the second beam splitter. It reflects off the second spherical concave mirror (the ocular), and is then reflected by
the second beam splitter and into the wearer’s eye. This arrangement provides a Keplerian (celestial, reversing) telescope and results in light loss due to 4 passes through the beam splitters. Four such passes will result in loss of $15/16$ (94%) of the entering light.

**Figure 6**: A schematic of a Keplerian (celestial-reversing) in-the-lens telescope using spherical mirrors, polarizing beam splitters and quarter wave plates.

**Figure 7**: Photo of the magnifying element using a polarizing beam splitter in the MicroOptical in-the-lens electronic display.

The light loss can be substantially recovered using polarizing beam splitters and quarter wave plates (Fig. 6). The first polarized beam splitter that reflects only the S-component results in a 50% loss of light. Following reflection in the objective curved mirror and passing twice through the quarter wave plate the reflected light will be polarized appropriately to pass almost
unaffected through the polarizing beam splitter. Assuming there is no change in the polarization state of the light as it travels through the carrier lens it will pass through the second polarized beam splitter with similar loss. Because of two passes through the quarter wave plate associated with the second mirror the light will then be reflected at the second beam splitter. Thus the total light loss can be limited to 50% in an ideal situation. In the practice, both reflection and transmission factors can be only about 80% efficient for the selected polarization state. After two reflections and two transmissions through the beams splitters, a total loss of light would be about 80% from natural light (0.5 × 0.8^4). Because the eye’s sensitivity is logarithmic, 80% loss of brightness should not significantly impact the utility of the telescope. The light loss can be compensated for, in part, by increasing the width of the objective lens providing more light collection, as discussed further below.

An additional advantage of the beam splitter design is that the semitransparent beam splitter is less visible than a regular mirror which results in better cosmetics. This advantage holds only for the objective. The ocular beam splitter should be provided with an opaque backing to improve the contrast of the image for the wearer. The reduced visibility of the objective makes it possible to make the objective larger and bring it closer to the ocular, as it will not block the view through the carrier lens. Thus, using a semi-transparent mirror allows the carrier lens to be made smaller as it removes the constraint that the objective mirror be placed out of the visual field of the wearer. The smaller carrier lens reduces system weight, and is also currently more fashionable. The ability to see through the objective area also allows for a wider objective, which can in part compensate for the light loss at the first beam splitter.

The opaque occluder can be achieved by providing a polarizer across the whole front of the lens. The polarizer will turn opaque for the ocular lens but will remain transparent for the objective lens. The light attenuation through the polarizer throughout the carrier lens may provide a glare control which will increase the comfort of the wearer and increase the relative brightness of the view through the telescope as compared to the view through the carrier lens.
A challenge to the beam splitter based approach, however, is that any birefringence in the carrier lens material can rotate the polarization of the light. The rotated light will then be reflected, rather than transmitted, in the first pass through the second beam splitter and will be lost from the system. Thus the carrier lens has to be as free as possible from birefringence effects.

To convert the celestial Keplerian telescope design (Fig. 6) to a terrestrial setup using beam splitters requires an erecting system. Fig. 8 illustrates one such design constructed by rotating the two assemblies around an axis through the carrier lens ultimately placing the spherical mirrors above the beam splitters. This design, similar to the basic Keplerian design (Fig. 4), uses the beam splitters as part of the image erecting system. Importantly, this design preserves the property that the width of the fields and the size of the objective are not limited by the thickness of the carrier lens.
Figure 8: Front and side views of the Keplerian design using polarizing beam splitters and spherical mirrors. Quarter wave plates (\(\lambda/4\)) are inserted between the beam splitters and the mirrors. Half of the light is lost at the first reflection in the beam splitter but ideally the quarter wave plate assures that the light reflected from the mirror is polarized to pass unaffected through the beam splitter. This light polarization causes no light to be lost through each pass in the second beam splitter. The occluder in front of the ocular beam splitter is required to block the see-through view and increase the contrast of the magnified image. The ocular and objective are shown at different vertical position on the carrier only to facilitate the side view illustration; they can be placed at the same height if needed.

2.5. Detailed Optical designs

ZEMAX software (ZEMAX Development Corp., Bellevue, WA) was used in simulation and ray tracing using actual components and specific dimensions. Reported computational results used the geometrical image analysis tool to evaluate FOV using various designs, and also allowed us to assess the image quality in terms of distortion and point spread function (PSF). Early prototypes were selected for construction based on the analysis performed in ZEMAX.
2.5.1. Keplerian design with off-axis parabolic mirrors

As described generically in section 2.3, we used 90° off-axis parabolic mirrors with radii 60mm and 20 mm for the objective and ocular respectively, providing an effective magnification of 3.0×. The “shape form” of the mirrors selected was 20mm horizontally and 5mm vertically (for a 5 mm thick carrier lens). Mirrors were embedded in a flat carrier lens of BK7 glass (Fig. 9a). This design resulted in a convenient eye relief of 15mm from the back surface of the carrier lens.

Image quality, in terms of PSF or modulation transfer function (MTF), was satisfactory in the central field, but degraded rapidly with eccentricity (Fig. 9b). Due to the rapid degradation of the image in the vertical direction, increasing the vertical dimension of the mirrors provided no effective increase in vertical field. The main effect illustrated by this analysis was the anisotropic distortion due to the differences in curvature that mirrors present to tilted rays (Fig. 9b). The distortion was confirmed in a prototype of this design which enabled us to experience the disturbing visual effect of the distortion (section 3.2).

![Figure 9: a) 3D layout and ray tracing of the off-axis parabolic mirror design showing eye pupil (P) and retina (R). Rectangles represent effective areas for the first and second surfaces of the carrier lens. b) Image from two square 5×5 grid objects, subtending 5° and 15° respectively. Notice the similarity of the distortion to that shown in Fig. 13.](image)
2.5.2. Keplerian design with beam splitters

This is the design described generically in section 2.4. Using a bi-planar carrier lens of 8mm thickness, the following design achieves a 1:2 format in the image field with an entrance pupil of 16mm horizontally and 8mm vertically. As described before, two polarizing beam splitters, in combination with thin quarter wave phase plates, allows the use of on-axis curved mirrors. These mirrors are obtained by mirroring the curved surfaces of a pair of conventional plano-convex lenses from Edmund Optics catalog (Edmund Optics Inc., Barrington, NJ), NT45-153 and NT45-360 models with 29.21mm and 38.76 mm of radius respectively. The 3D layout of this design with the lens configuration described is shown in Fig. 10a. The magnification obtained is 3.33× and an emergence or eye relief of 10mm from the last surface. Fig. 10b shows the final retinal image of two square 5×5 grid objects, subtending 5° and 20° respectively, to show the vigneting field extension. The image distortion problem is satisfactorily solved, since on axis spherical mirrors are used.

Figure 10: a) 3D layout and ray tracing of the polarizing beam splitter design showing eye pupil (P) and 8 mm think carrier lens. b) Image from two square 5×5 grid object, subtending 5° and 20° respectively. Notice the reduction of distortion compared to parabolic mirrors design.
3. Prototypes

To assess the feasibility of the in-the-lens telescope concept we have constructed and evaluated a series of preliminary prototypes.

3.1. Keplerian design with laminated lenses

In the first prototype we implemented the generic design shown in section 2.2. The lower image erecting mirrors were achieved by cutting an ophthalmic lens blank. The periscopic mirrors were achieved using small prisms. All mirroring was achieved in this design through total internal reflection as shown in Fig. 11.

Figure 11: a) A back vertex and b) side view of the crude prototype of the telescope illustrated in Fig. 4. The telescope was constructed from an ophthalmic lens blank cut to provide the erecting mirrors through total internal reflection. Off the shelf ocular and objective lenses provided the magnification and small right angle prisms served as the periscopic mirrors (M1 and M4 in Fig. 4a).
Fig. 12 is an image photographed through the prototype shown in Fig 11. The magnified image of the CVS sign is seen at the same time as the unmagnified view of the sign obtained through the carrier lens. This illustrates the possibility of spatial multiplexing by shifting. In this case the image shift was achieved by tilting the whole lens assembly relative to the camera. This tilt resulted in blurring of the magnified image. A much better image quality of the CVS sign was obtained in direct (non-tilted) view through the telescope (not shown).

Figure 12: An image photographed through the first prototype shown in Fig 11. The magnified image of the CVS sign is shown above and to the right of the unmagnified view of the sign obtained through the carrier lens, illustrating spatial multiplexing by shifting. The shift was obtained by tilting the whole lens assembly relative to the camera, which resulted in blurred magnified image.

3.2. Off-axis parabolic mirrors design

A second generation prototype of the telescope was built using off-axis parabolic mirrors as described in section 2.3. This prototype used 30-deg off axis metal mirrors (Edmund Optics) which were on hand. The prototype provided satisfactory image quality and validated the approach. The system exhibited a moderate level of distortion. The distortion was hardly
noticeable on a static image of a building that provided a good grid structure. However, the distortion became noticeable as the telescope was moved. A second prototype was constructed using 90-deg off axis mirrors (NT47-100: Diameter 25.4mm, EFL 101.6mm and NT47-098: Diameter 25.4mm, EFL 50.8mm) resulting in a 2.0× Keplerian telescope. This prototype did not include the erecting mirrors; therefore, it provided an inverted image (Fig 13). Also the layout was horizontal, so the main distortion appears tilted 90 deg clockwise relative to that illustrated in Fig 9b.

![Figure 13: The view through a 2.0× Keplerian telescope created with two 90-deg. off axis parabolic mirrors. a) A view of a building across the street. b) The view of the same building through the telescope showing a clear magnified inverted image of the crane and significant distortion in the vertical meridian. The color of the image is a result of the gold coating of the mirrors.](image)

4. **Additional considerations**

4.1. **Field-of-view**

The ocular lens (mirror) of the in-the-lens telescope is likely to be rectangular in shape. In the horizontal dimension, the only limitations on the lens size are: the dimension of the lens
itself, the spectacle frame, and the value chosen for the telescope length, \( L \). The vertical extent of the lenses, however, is limited by the carrier lens thickness \( t \). The embedded ocular mirror (\( M4 \) in Fig. 8) would be the field stop, and we can approximate the restriction to its vertical size as being less than or equal to \( t \). A reasonable range of carrier lens thickness would be 5 to 10mm. For example, a thickness of 10mm with a 10mm for eye relief allows a vertical visual field up to 53° in the image space (on the retina), which translate to approximately 18° in object space, 50% wider than most existing bioptic telescopes. The horizontal field-of-view (which is less restricted) may be as much as twice as wide as the vertical dimension. The horizontal extent of the field-of-view is usually considered more important for navigation and reading, so even thinner carrier lenses would be acceptable.

4.2. **Light economy**

The dimensions chosen for the carrier lens (e.g. thickness) limit the dimensions of the objective lenses, which in turn also determine the size of the exit pupil. The exit pupil size is important in determining the light efficiency of the telescope. When the exit pupil completely covers the eye’s pupil the light efficiency is maximal at 100%. As stated above, the carrier lens thickness limits the vertical extent of the objective and thus, the exit pupil. However, the horizontal extent can be much larger and is not constrained by the thickness, resulting in a wide rectangular shaped objective. The exit pupil, the image of the objective aperture through the ocular, will also have the dimension of the objective divided by the magnification. For example, an entrance pupil of 16mm×8mm (carrier lens 8mm thick), with a magnification of 3.3×, yields an exit pupil of 4.8mm×2.4mm. These dimensions may limit the amount of light entering the eye due to pupil coupling (mainly in the vertical dimension) ⁴⁰. For the same example, assuming an eye pupil of 3mm, the maximum light efficiency is 90% (Fig. 14a), while with an eye pupil of 4mm, the light efficiency is reduced below 72% (Fig. 14b). The extended horizontal dimension
in the objective (which is possible) improves the light collection of the telescope when the pupil is enlarged (in dim light condition).

![Diagram of effective pupil shapes](image)

Figure 14: Examples of the effective pupil due to the rectangular shape of exit pupil. Dashed rectangles represent the same size exit pupil compared with 2 different eye pupil diameters. The light gain (or actual loss) is equal to the percentage of area of the eye pupil covered by the exit pupil, as shown in the diagrams.

The overlap between the exit pupil and the eye’s pupil may also be reduced by scanning eye movements, taking the pupil away from the center of the exit pupil. Since most eye movements, especially with a wider horizontal field-of-view, are horizontal, the wider horizontal extent of the exit pupil protects the light efficiency during eye movements. Thus a wider objective is desirable even if the wider field-of-view was not necessary.

We computed the effects of the carrier lens thickness on the maximal possible light efficiency due to the exit pupil coupling. Fig. 15 shows the results for an eye centered on the exit pupil in a telescope of magnification 2.8×, as a function of the selected thickness for the carrier lens, and for various eye pupil diameters. For the calculation, the horizontal dimension of the objective was considered always 20mm wide. Older people would present small pupil diameters (about 3mm in diameter) while large pupils would be expected for young wearers under dim light conditions.
Figure 15: The influence of the carrier lens thickness in a Keplerian telescope of magnification 2.8× on the light loss due to exit pupil coupling for several eye pupil diameters. Horizontal dimension of the objective element was considered fixed to 20mm.

4.3. **Refractive Correction**

As eyewear, the in-the-lens telescope must provide refractive correction for the wearer both through the telescope and through the carrier lens. All our diagrams have illustrated the carrier lens as a flat lens on both sides and thus could be used only by emmetropes. A refractive correcting lens could be laminated to the back surface of the lens or be grounded into that surface. Such a correction will apply equally to the telescope and the carrier. A standard ophthalmic lens blank is usually provided as a meniscus lens with a front convex surface (base curve). The positive front base curve is needed for better cosmetics and for improved optical performance. The refractive correction is typically applied using widely available equipment to grind the back surface of the lens blank. The same approach can be easily applied to the in-the-lens telescope. The lens blank for this telescope may be developed with a fairly flat base curve.
The telescope optical tube length needs to be slightly modified from the afocal configuration to result in a vergence at the second beam splitter which is identical to that created by the base curve at the back surface. With such a blank, the back surface may be grounded to the wearer’s prescription on the back surface using standard ophthalmic lab techniques and equipment. The correction applied to the carrier lens will result in a proper correction for the telescope as well. This would make such a lens easily dispensable in every ophthalmic shop. Tilts generated in the objective and the ocular due to the prismatic effect of the carrier lens (Percival’s Rule) can be compensated by centering the curved surfaces on each beam splitter, if needed. Alternately, the prismatic effect may be used to support vision multiplexing.

A side effect of using a curved carrier lens is that the magnification is slightly reduced compared with the plano-parallel carrier lens equivalent, using the same curved mirrors. The reason for such an effect can be easily described as an increase of the objective lens power and a reduction of the ocular power due to the curved carrier surfaces. Thus, the magnification as the ratio of both refractive powers is reduced. To quantify the effect, we simulated the same model described in Fig. 10 embedded in three carrier lenses with base curve surfaces of 0, 1, and 3 diopters, resulting in angular magnifications of 3.3×, 3.2×, and 3.0×, respectively.

5. Discussion

We have described a novel design for bioptic telescopes. We have proposed and tested a family of possible designs for Galilean and Keplerian telescopes using either laminated lenses, embedded curved mirrors, or polarizing converging beam splitters. We have analyzed these designs through computer simulations and prototyped the designs to demonstrate the feasibility of such devices. These analyses provide insight to the following qualities: magnification, image quality, field-of-view, distortion, and their utility in vision multiplexing.

Biotic telescopes are the most efficient visual aid available for distance vision, yet they are commonly rejected by people with low vision due to their appearance. Our approach
addresses this point of contention while maintaining visual performance similar to or better than current bioptics. Although the in-the-lens telescope is not cosmetically invisible, its compactness and internalized components attracts less attention than current designs. Figure 16 shows a conceptual simulation of the appearance of the in-the-glass Keplerian telescope.

![Figure 16: Simulation of the expected appearance of the in-the-lens telescope.](image)

The proposed in-the-lens telescope can be used to simultaneously view the magnified image and the unmagnified image of the same area. This vision multiplexing feature improves wearer orientation and navigation. The wearer can easily locate an object or determine the relative position of the object. The spectacle lens can include the wearer’s correcting prescription. We believe that these features will make this device very desirable and that the ability to incorporate the wearer’s prescription using standard ophthalmic procedure will control the cost of the device and will support its wide distribution.

**ACNOWLEDGMENTS**

Supported in part by NIH grant EY 12890. F. Vargas-Martín has received a travel grant from Fundación Séneca, (Murcia, Spain). We thank Morey Waltuck for help with the construction of the Keplerian design with laminated lenses and, Gang Luo for help with the construction of the off-axis parabolic mirrors prototype.
REFERENCES


FIGURE CAPTIONS

Figure 1: A monocular Galilean bioptic telescope. a) Most of the time the wearer views through the carrier lens without any effect of the telescope. b) With a slight downward tilt of the head the telescope is brought into the line of sight enabling magnified view of the object of interest. The telescope shown is the 3.0× Mini focusable Keplerian bioptic made by Ocutech, Inc. (Chapel Hill, NC)

Figure 2: A simulated view of a road sign viewed through a 3.0× telescope. a) The view through a conventional bioptic. The magnified image on the retina blocks the view of much of the intersection creating a ring scotoma (blind area). b) The rectangle field-of-view through the in-the-lens telescope. The magnified image is shifted up blocking part the view of the pedestrian bridge overhead but leaves the intersection in full view. Note the non magnified view of the road sign seen under the magnified view. The white line surrounding the magnified image is only added to make the illustration more clear.

Figure 3: a) A basic schematic design of the in-the-lens telescope with a spectacle lens of thickness, t seen from above. For the Galilean design a positive objective lens and a negative ocular lens are laminated to the carrier lens. Two mirrors serve to periscopically pass the image from the objective to the ocular. b) An illustration of the in-the-lens when the wearer looks though the carrier lens. c) The same lens following a head tilt that brings the telescope in front of the pupil. Note the thin and tall shape of the telescopic mirrors due to the limitation by the carrier lens thickness on the width of the mirrors.

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Figure 4: a) Side view of the Keplerian telescope with laminated lenses and four flat erecting mirrors. b) Front view illustration of the Keplerian design telescope that emphasizes the wide but short configuration of the mirrors and their corresponding field-of-view. In this design the carrier lens thickness limits the height but not the width of the objective and ocular mirrors.

Figure 5: Top, front, and side views schematic of the in-the-lens telescope using only mirrors embedded in the carrier lens. Curved off-axis parabolic mirrors (M1 & M4) for power and flat mirrors (M2 & M3) for the second image inversion.

Figure 6: A schematic of a Keplerian (celestial-reversing) in-the-lens telescope using spherical mirrors, polarizing beam splitters and quarter wave plates.

Figure 7: Photo of the magnifying element using a polarizing beam splitter in the MicroOptical in-the-lens electronic display.

Figure 8: Front and side views of the Keplerian design using polarizing beam splitters and spherical mirrors. Quarter wave plates (λ/4) are inserted between the beam splitters and the mirrors. Half of the light is lost at the first reflection in the beam splitter but ideally the quarter wave plate assures that the light reflected from the mirror is polarized to pass unaffected through the beam splitter. This light polarization causes no light to be lost through each pass in the second beam splitter. The occluder in front of the ocular beam splitter is required to block the
see-through view and increase the contrast of the magnified image. The ocular and objective are shown at different vertical position on the carrier only to facilitate the side view illustration; they can be placed at the same height if needed.

Figure 9: a) 3D layout and ray tracing of the off-axis parabolic mirror design showing eye pupil (P) and retina (R). Rectangles represent effective areas for the first and second surfaces of the carrier lens. b) Image from two square 5×5 grid objects, subtending 5° and 15° respectively. Notice the similarity of the distortion to that shown in Fig. 13.

Figure 10: a) 3D layout and ray tracing of the polarizing beam splitter design showing eye pupil (P) and 8 mm think carrier lens. b) Image from two square 5×5 grid object, subtending 5° and 20° respectively. Notice the reduction of distortion compared to parabolic mirrors design.

Figure 11: a) A back vertex and b) side view of the crude prototype of the telescope illustrated in Fig. 4. The telescope was constructed from an ophthalmic lens blank cut to provide the erecting mirrors through total internal reflection. Off the shelf ocular and objective lenses provided the magnification and small right angle prisms served as the periscopic mirrors (M1 and M4 in Fig. 4a).

Figure 12: An image photographed through the first prototype shown in Fig 11. The magnified image of the CVS sign is shown above and to the right of the unmagnified view of the sign obtained through the carrier lens, illustrating spatial multiplexing by shifting. The shift was obtained by tilting the whole lens assembly relative to the camera, which resulted in blurred magnified image.
Figure 13: The view through a $2.0 \times$ Keplerian telescope created with two 90-deg. off axis parabolic mirrors. a) A view of a building across the street. b) The view of the same building through the telescope showing a clear magnified inverted image of the crane and significant distortion in the vertical meridian. The color of the image is a result of the gold coating of the mirrors.

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Figure 15: The influence of the carrier lens thickness in a Keplerian telescope of magnification $2.8 \times$ on the light loss due to exit pupil coupling for several eye pupil diameters. Horizontal dimension of the objective element was considered fixed to 20mm.

Figure 16: Simulation of the expected appearance of the in-the-lens telescope.
Ø 3mm 90%

Ø 4mm 72%